

**MODUL PINTAS PPC PAHANG SPM 2023**

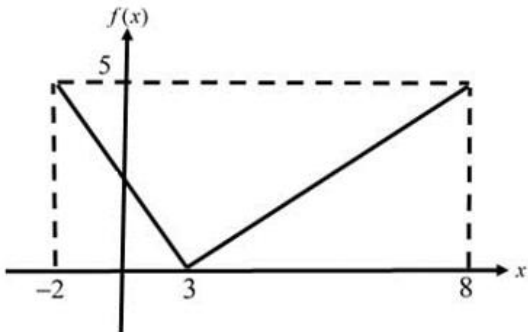
**MATEMATIK TAMBAHAN  
PERATURAN PEMARKAHAN**

**KERTAS 1**

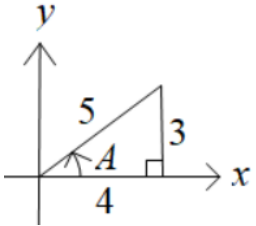
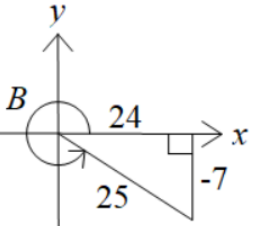
| SOALAN   |                              | SKEMA   | MARKAH | MARKAH PENUH |
|----------|------------------------------|---|--------|--------------|
| <b>1</b> |                              | Cari $m$<br>$\frac{13-3}{8-3}$ atau setara  | 1      |              |
|          |                              | Cari $c$<br>$13 = *2(8) + c$ atau<br>$3 = *2(3) + c$ atau<br>$Y - 13 = *2(X - 8)$ atau<br>$Y - 3 = *2(X - 3)$ | 1      |              |
|          |                              | $\ln y = 2 \ln x - 3$   | 1      |              |
|          |                              | $y = \frac{x^2}{e^3}$ atau $y = \frac{x^2}{20.09}$ atau $y = 0.04979x^2$                                      | 1      |              |
|          |                              |   |        |              |
|          |                              |   |        | <b>4</b>     |
| <b>2</b> | (a)                          | (i) $m^{-1}(x) = x - 5$ <b>atau</b> $m(-2) = 3$   | 1      |              |
|          |                              | $(t + 2) - 5 = 3$   | 1      |              |
|          |                              | 6   | 1      |              |
|          | (ii) $nm(x) = (x + 5)^2 - 2$ | 1   |        |              |
|          | (b)                          | (i) $\frac{p}{y} + 2 = x$ , $y$ boleh sebarang huruf selain $x, k, g, p$                                      | 1      |              |
|          |                              | $g(y) = \frac{5\left(\frac{p}{y} + 2\right) - 8}{\left(\frac{p}{y} + 2\right) - 2}$                           | 1      |              |
|          |                              | $g(x) = \frac{5p + 2x}{p}$ <b>atau</b> $g(x) = 5 + \frac{2}{p}x$  | 1      |              |
|          |                              | (ii) 7  | 1      |              |
|          |                              |   |        | <b>8</b>     |

|   |     |   |   |   |
|---|-----|---|---|---|
| 3 | (a) | $\alpha + \beta = \frac{p}{2}$  | 1 | 6 |
|   |     | $\alpha\beta = \frac{q}{2}$   | 1 |   |
|   | (b) | $\frac{2}{\alpha} + \frac{2}{\beta} = -\frac{-12}{3}$ dan $\left(\frac{2}{\alpha}\right)\left(\frac{2}{\beta}\right) = \frac{8}{3}$ | 1 |   |
|   |     | $\frac{4}{\frac{q}{2}} = \frac{8}{3}$   | 1 |   |
|   |     | Gantikan nilai $q$ :<br>$\frac{2\left(\frac{p}{2}\right)}{\frac{*3}{2}} = \frac{-(-12)}{3}$   | 1 |   |
|   |     | $q = 3, p = 6$  | 1 |   |
| 4 | (a) | $q - (q+3) = (q+3) - (3q-2)$  | 1 | 5 |
|   |     | $q = 4$   | 1 |   |
|   | (b) | $a = 10$ dan $d = -3$   | 1 |   |
|   |     | $S_{14} - S_6$<br>$\frac{14}{2}[2(10) + (14-1)(-3)] - \frac{6}{2}[2(10) + (6-1)(-3)]$<br>atau setara                                | 1 |   |
|   |     | -148  | 1 |   |
|   |     |   |   |   |
| 5 | (a) | (i) $\frac{4}{n+1}x^{n+1} + c$  | 1 | 5 |
|   |     | (ii) $n \neq -1$  | 1 |   |
|   |     | $c =$ pemalar pengamiran  | 1 |   |
|   | (b) | $\frac{25x^{-3}}{-3} - \frac{x^{-1}}{-1}$   | 1 |   |
|   |     | $-\frac{25}{3x^3} + \frac{1}{x} + c$  | 1 |   |
|   |     |   |   |   |

|          |      |     |   |   |          |   |
|----------|------|-----|---|---|----------|---|
| <b>6</b> |      |     | $10\theta = \frac{25}{9}\pi$  | 1   |          |   |
|          |      |     | $\frac{5}{18}\pi$   | 1   |          |   |
|          |      |     |   |   | <b>2</b> |   |
| <b>7</b> | (a)  |     | $\frac{11!}{4!4!2!}$  | 1   |          |   |
|          |      |     | 34650   | 1   |          |   |
|          | (b)  | (i) |   | ${}^3C_1 \times {}^2C_1$ <b>atau</b> ${}^2C_1 \times {}^2C_1$ <b>atau</b> ${}^2C_1 \times {}^2C_1$  |          | 1 |
|          |      |     |   | $({}^3C_1 \times {}^2C_1) + ({}^2C_1 \times {}^2C_1) + ({}^2C_1 \times {}^2C_1)$  |          | 1 |
|          |      |     |   | 14  |          | 1 |
|          | (ii) |     |   | $(6-1)!$ atau setara  |          | 1 |
|          |      |     |   | 120   |          | 1 |
|          |      |     |   |   |          |   |
|          |      |     |   |   | <b>7</b> |   |
| <b>8</b> | (a)  |     | $(11,13) = \left( \frac{1(x)+2(14)}{1+2}, \frac{1(y)+2(11)}{1+2} \right)$ | 1   |          |   |
|          |      |     | $K = \left( \frac{1(2)+2(*5)}{1+2}, \frac{1(2)+2(*17)}{1+2} \right)$      | 1   |          |   |
|          |      |     | $K(4,12)$   | 1   |          |   |
|          | (b)  |     |   | $\frac{1}{2}  (5(13)+11(12)+4(17)) - (17(11)+13(4)+12(5)) $<br><b>atau</b><br>$\frac{1}{2}  (2(11)+14(13)+11(12)+4(2)) - (2(14)+11(11)+13(4)+12(2)) $ |          | 1 |
|          |      |     |   | 17 dan $\frac{119}{2}$ @ 59.5   |          | 1 |
|          |      |     |   | 2:7   |          | 1 |
|          |      |     |   |   |          |   |
|          |      |     |   |   | <b>6</b> |   |
| <b>9</b> | (a)  |     | $a = 22680$ , $r = \frac{9}{16}$  | 1   |          |   |
|          |      |     | $22680 \left( \frac{9}{16} \right)^{n-1} < 100$                           | 1   |          |   |

|           |     |  |   |   |          |
|-----------|-----|--|---|---|----------|
|           |     |  | $n-1 > \frac{\log_{10} \frac{100}{22680}}{\log_{10} \frac{9}{16}}$  | 1 |          |
|           |     |  | $n = 11$  | 1 |          |
|           | (b) |  | $\frac{22680}{1 - \frac{9}{16}}$  | 1 |          |
|           |     |  | 51840   | 1 |          |
|           |     |  |   |   | <b>6</b> |
| <b>10</b> |     |  | $V = \pi j^3$   | 1 |          |
|           |     |  | $\partial V = -0.6 \text{ cm}^3$  | 1 |          |
|           |     |  | $\frac{dV}{dj} = 3\pi j^2$  | 1 |          |
|           |     |  | Guna rumus $\partial V = \frac{dV}{dj} \times \partial j$ dan gantikan nilai<br>$-0.6 = 3\pi(3.1)^2 \times \partial j$        | 1 |          |
|           |     |  | $\partial j = -0.006624 // -0.006625 // -\frac{20}{961\pi}$   | 1 |          |
|           |     |  |   |   | <b>5</b> |
| <b>11</b> | (a) |  | ${}^n C_5 (0.4)^5 (0.6)^{n-5} = 10 [{}^n C_4 (0.4)^4 (0.6)^{n-4}]$  | 1 |          |
|           |     |  | $\frac{n!}{(n-5)!5!} (0.4)^5 \frac{(0.6)^n}{(0.6)^5} = 10 \left[ \frac{n!}{(n-4)!4!} (0.4)^4 \frac{(0.6)^n}{(0.6)^4} \right]$ | 1 |          |
|           |     |  | $n = 79$  | 1 |          |
|           | (b) |  | Min = 31.6  | 1 |          |
|           |     |  |   |   | <b>4</b> |
| <b>12</b> | (a) |  |   |   |          |

|           |     |       |   |   |          |
|-----------|-----|-------|---|---|----------|
|           |     |       | Bentuk V  | 1 |          |
|           |     |       | Label $(3,0), (-2,5), (8,5)$  | 1 |          |
|           |     |       | Julat: $0 \leq f(x) \leq 5$   | 1 |          |
|           | (b) |       | $fg(x) =  2x-9 $  | 1 |          |
|           |     |       | $2x-9 = x, 2x-9 = -x$   | 1 |          |
|           |     |       | $x = 9, x = 3$  | 1 |          |
|           |     |       |   |   | <b>6</b> |
| <b>13</b> | (a) | (i)   | $\overrightarrow{BC} = \overrightarrow{AC} - \overrightarrow{AB}$ @ setara<br><b>ATAU</b><br>$\overrightarrow{AT} = \overrightarrow{AB} + \overrightarrow{BT}$ @ setara | 1 |          |
|           |     |       | $\overrightarrow{BC} = -2\underset{\sim}{i} + 10\underset{\sim}{j}$ atau $\begin{pmatrix} -2 \\ 10 \end{pmatrix}$   | 1 |          |
|           |     | (ii)  | $\overrightarrow{AT} = \frac{7}{2}\underset{\sim}{i} - \frac{7}{2}\underset{\sim}{j}$ atau $\begin{pmatrix} 7 \\ 2 \\ -\frac{7}{2} \end{pmatrix}$                       | 1 |          |
|           |     |       | $\frac{\frac{7}{2}\underset{\sim}{i} - \frac{7}{2}\underset{\sim}{j}}{\sqrt{\left(\frac{7}{2}\right)^2 + \left(-\frac{7}{2}\right)^2}}$                                 | 1 |          |
|           |     |       | $\frac{\sqrt{2}}{2}\underset{\sim}{i} - \frac{\sqrt{2}}{2}\underset{\sim}{j}$   | 1 |          |
|           |     | (iii) | $-3\underset{\sim}{i} + k\underset{\sim}{j} = -2h\underset{\sim}{i} + 10h\underset{\sim}{j}$  | 1 |          |
|           |     |       | $h = \frac{3}{2}$   | 1 |          |
|           |     |       | $k = 15$  | 1 |          |
|           |     |       |   |   | <b>8</b> |
| <b>14</b> | (a) | (i)   | $\log_a x = p, x = a^p$ <b>atau</b> $\log_a y = q, y = a^q$   | 1 |          |
|           |     |       | $\frac{x}{y} = a^{p-q}$   | 1 |          |
|           |     |       | $\log_a \frac{x}{y} = \log_a x - \log_a y$  | 1 |          |

|    |      |   |   |   |   |
|----|------|---|---|---|---|
| 15 | (b)  | (ii)  | Guna hukum hasil bahagi: $\log_3\left(\frac{54}{6} \div 3\right)$   | 1 |   |
|    |      |   | 1   | 1 |   |
|    |      |   | $20\,000e^{-0.03t} < \frac{1}{2}(20\,000)$  | 1 |   |
|    |      |   | $t > \frac{\ln \frac{1}{2}}{-0.03}$   | 1 |   |
|    |      | 24  | 1   | 8 |   |
|    |      |   |   |   |   |
|    | (a)  | (i)   | $495^\circ$   | 1 | 8 |
|    |      | (ii)  | $\frac{2}{-\sin \theta}$  | 1 |   |
|    |      |   | $-\frac{2}{h}$  | 1 |   |
|    | (b)  | (i)   | $\sin A = \frac{3}{5} @ \cos A = \frac{4}{5} @$ <br>ATAU<br>$\sin B = -\frac{7}{25} @ \cos B = \frac{24}{25} @$  | 1 |   |
|    |      | $\left(\frac{3}{5}\right)\left(\frac{24}{25}\right) + \left(\frac{4}{5}\right)\left(-\frac{7}{25}\right)$ | 1   |   |   |
|    |      | $\frac{44}{125}$  | 1   |   |   |
|    | (ii) | $\frac{\frac{3}{4} - \left(-\frac{7}{24}\right)}{1 + \left(\frac{3}{4}\right)\left(-\frac{7}{24}\right)}$ | 1   |   |   |
|    |      | $\frac{4}{3}$   | 1   |   |   |
|    |      |   |   |   |   |